## On chromatic uniqueness of certain 5-partite graphs

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Abstract Let  $P(G, \lambda)$  be the chromatic polynomial of a graph *G*. Two graphs *G* and *H* are said to be chromatically equivalent, denoted  $G \sim H$ , if  $P(G, \lambda) = P(H, \lambda)$ . We write  $[G] = \{H \mid H \sim G\}$ . If  $[G] = \{G\}$ , then *G* is said to be chromatically unique. In this paper, we first characterize certain complete 5-partite graphs with 5n + 3 vertices according to the number of 6-independent partitions of *G*. Using these results, we investigate the chromaticity of *G* with certain star or matching deleted. As a by-product, many new families of chromatically unique complete 5-partite graphs with certain star or matching deleted are obtained.

Keywords Chromatic polynomial · Chromatically closed · Chromatic uniqueness

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## **1** Introduction

All graphs considered here are simple and finite. For a graph *G*, let  $P(G, \lambda)$  be the chromatic polynomial of *G*. Two graphs *G* and *H* are said to be *chromatically equiv*alent (or simply  $\chi$ -equivalent), symbolically  $G \sim H$ , if  $P(G, \lambda) = P(H, \lambda)$ . The equivalence class determined by *G* under  $\sim$  is denoted by [*G*]. A graph *G* is *chromatically unique* (or simply  $\chi$ -unique) if  $H \cong G$  whenever  $H \sim G$ , i.e,  $[G] = \{G\}$ 

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