

ISSN: 1991-8941

STUDYING THE NUCLEAR STRUCTURE OF EVEN-EVEN DEFORMED GERMANIUM $^{70}_{32}\text{Ge}_{38}$ NUCLEUS

ALI KALAF AOBAID

DEPT. OF PHYSICS-COLLEGE OF EDUCATION-AL-ANBAR UNIVERSITY

Received :8/3/2007

Accepted:13/12/2007

Abstract

In the present work, the interacting boson model(IBM-1) for s and d boson is used to calculate the energy levels of the positive parity bands, electric quadrupole moments, E2-transition probabilities B(E2)in particular between states which may be affected by the finite boson number $N=N_{\pi}+N_{\nu}=2+5=7$ of even-even $^{70}_{32}\text{Ge}_{38}$ nucleus . This nucleus is belong to SU(5)-SU(3) dynamical symmetry .

The calculated results of this study are compared with the available experimental data and they found to be in a very good agreement.

Keywords: nuclear structure , even-even deformed Germanium $^{70}_{32}\text{Ge}_{38}$ nucleus

Introduction

In 1974 Arima A. and Iachello F. have proposed a new nuclear model, called ; Interacting Boson Model (IBM); [1],which attempts to describe some nuclear properties such as spins and energies of the lowest levels of intermediate and heavy mass nuclei, except those near closed shells[2,3].The simplest versions of IBM called; IBM-1; has to be able to describe the even-even deformed nuclei as an inert core combined with bosons which represent pairs of fermions , which can occupy one of two levels: a ground state with (L=0)called s-boson or an excited state with(L=2)called d-bosons[4].

The dynamical symmetries in this model are depending on the main group U(6) of unitary transformations in 6-dimansions and 36 generators. The analysis of this group leads to three subgroups called chains that end in O(2). They can be written as[3]:

(I) The vibrational SU(5)chain

$$U(6) \supset SU(5) \supset O(5) \supset O(3) \supset O(2) \dots (1)$$

(II) The rotational SU(3)chain:

$$U(6) \supset SU(3) \supset O(3) \supset O(2) \dots (2)$$

(III) The γ -unstable O(6)chain:

$$U(6) \supset O(6) \supset O(5) \supset O(3) \supset O(2) \dots (3)$$

One of the basic properties of deformed nuclei is the presence of specific collective rotational states SU(3) in their excitation spectra. These states can only be observed in nuclei with a non-spherical shape [5].

The collective motion of deformed nuclei depends on two facts [6,7]:

1-All deformed nuclei have an electric quadrupole moments in their energy states .

2-The changing in the deformation shape depends on the direction of nucleons and nuclear motion causing rotation of some nucleons around an axis different from nuclear symmetry axis , for this

reason, we can explain two types of deformation as follows:

1-Prolate deformation:

In this deformation, the nucleus rotate around an axis perpendicular to the nuclear symmetry axis . This type has positive quantity of electric quadrupole moment (+QL).

2-Oblete deformation:

In this deformation, the nucleus is rotating in axis parallel to the nuclear symmetric axis. This rotating happened in spherical nuclei , and it has negative quantity of electric quadrupole moment (-QL).Some of the previous studies about this subject are:

Iman T. AL-Alawy(2000)[8],had been calculate the (EO,E2,B(E2),QL) transitions of collective levels of Pt-196 nucleus.

Iman T. AL- Alawy, et al (2005) [9]had studied the electric quadrupole moments, and g-factor for deformed Yb(A=176)nucleus of dynamical symmetry SU(3)-SU(5).

Aobaid A.K.(2006)[10] studied the nuclear structure of some even-even

(⁵⁶Fe₃₀, ⁷⁴Se₄₀, ⁸⁸Zr₄₈, ¹⁰⁶Pd₆₀, ¹⁵⁶Gd₉₂, ¹⁸⁰Hf₁₀₈, ¹⁸⁶W₁₁₂) nuclei. He found a good agreement results with available experimental data.

Theoretical Part:

1-The Hamiltonian Operators In IBM-1:

Scholten, Iachello and Arima (1978) [11] proposed a simplest Hamiltonian form as follows:

$$\hat{H} = \varepsilon \hat{n}_d + b_0 (\hat{P}^\dagger \cdot \hat{P}) + b_1 \hat{L}^2 + b_2 \hat{Q} + b_3 \hat{T}_3^2 + b_4 \hat{T}_4^2 \dots \dots \dots (4)$$

Where:

ε is the energy parameter of d-boson operator (\hat{n}_d) , b_0 is the parameter of the pairing operator (\hat{P}) , b_1 is the parameter of the angular momentum operator (\hat{L}), b_2 is the parameter of the quadrupole momentum operator(\hat{Q}), b_3 is the parameter of the

octupole operator (\hat{T}_3), b_4 is the parameter of the hexadecapole operator (\hat{T}_4) .

The Hamiltonian in equation (4) depends on the type of dynamical symmetry as in equations (1,2,3)and takes the following form[3,4]:

for chain (I) :

$$\hat{H}^{(I)} = \varepsilon \hat{n}_d + b_1 \hat{L}^2 + b_3 \hat{T}_3^2 + b_4 \hat{T}_4^2 \dots (5)$$

for chain (II) :

$$H^{(II)} = b_1 \hat{L}^2 + b_2 \hat{Q}^2 \dots (6)$$

for chain (III) :

$$H^{(III)} = b_0 (\hat{P}^\dagger \cdot \hat{P}) + b_1 \hat{L}^2 + b_3 \hat{T}_3^2 \dots (7)$$

The electric transition operator, which is associated with collective states can be written as [4]:

$$\hat{T}(E2) = \delta_0 [\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}] + \delta_1 [\hat{d}^\dagger \times \hat{d}] \dots (8)$$

This operator has two parts [$\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}$] which satisfies the selection rule $\Delta n_d = \pm 1$, and the term [$\hat{d}^\dagger \times \hat{d}$] which satisfies the $\Delta n_d = 0$ selection rule .

The parameters δ_0 and δ_1 depend on the limit involved or the appropriate intermediate structure .

The electric transition operator T(E2) in equation (8) can be written down as[3] :

$$\hat{T}(E2) = e_B [(\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}) + \chi (\hat{d}^\dagger \times \hat{d})]^{(2)} = e_B Q \dots (9)$$

Where e_B is a boson effective charge , χ is any parameter.

The electric transition probability B(E2) determined from the following reduced matrix element [4]:

$$\langle LM_L || \hat{T}_K^{(K)} || L'M_L \rangle = (-1)^{L-M} \begin{pmatrix} L & K & L' \\ -M_L & K & M'_L \end{pmatrix} \langle L | \hat{T}^{(K)} | L' \rangle \dots (10)$$

The calculation of electric quadrupole moments for three chains depended on selected rules as shown in table (1), and can be written as:

$$Q_L = 0.676 \begin{pmatrix} L & 2 & L \\ -L & 0 & L \end{pmatrix} \langle L_f || \hat{T}^{(E2)} || L_i \rangle \dots (11)$$

While the electric transition probability $B(E2)$ can be written as:

$$B(E2; L_i \rightarrow L_f) = \frac{1}{(2L+1)} | \langle L_f || \hat{T}^{(E2)} || L_i \rangle |^2 \dots (12)$$

Results and Discussions:

1-The energy levels , and Their Transitions:

In order to calculate the nuclear structure of even-even ${}^{70}_{32}\text{Ge}_{38}$ deformed nucleus, we must find the dynamical symmetry of this nucleus. The dynamical symmetry for any nucleus was determined according to the following[4]:

1-Energy ratios as shown in table(2).

2-Experimental energy spectrum see references [3,4].

3-Energy band arrangement(g, β , γ)

Table (2) listed the calculated energy ratios (pw) in comparison with experimental [12,13] and ideal [3] values . This table shows the nucleus under study lying in the transitional region SU(5)-SU(3), also this table gives very reasonable description of the behavior ${}^{70}_{32}\text{Ge}_{38}$ nucleus.

The parameters of Hamiltonian equation (4) for ${}^{70}_{32}\text{Ge}_{38}$ nucleus are shown in table (3).

These parameters have been obtained by fits them with experimental energy levels values for low spin and used to calculate the energy levels and their transitions as in table(4)

Table(4) shows a good comparison between calculated energy levels and available experimental values ,specially at low-lying of the ground states ($0_1^+, 2_1^+, 4_1^+, 6_1^+, 8_1^+$),and in other states ($2_3^+, 0_3^+, 2_4^+, 4_2^+, 2_5^+, 4_3^+, 4_4^+, 4_5^+, 2_7^+, 4_7^+$) while at high angular momentum, some theoretical values are somehow larger than experimental because:

1-These values need large time to be measured.

2-The IBM-1 does not distinguish between neutrons and protons bosons.

3-The fitted of equation (4) was very difficult to get same values as experimental data for all energy levels.

2-The electric Transitions Probability B(E2):

In this work, the equations (10,12) are used to calculate the electric transition probability and their reduced matrix element for this deformed nucleus .The parameters for these equations are ($\delta 0=0.10498(\text{eb})$, and $\delta 1=0.068(\text{eb})$). These parameters have been obtained by fitting them with experimental values of $B(E2)$.

The calculated results are listed in table (4). This table contain the comparison between calculated $B(E2)$ and available experimental data. The comparison shows an acceptable agreement, specially at transitions ($2_1^+ \rightarrow 0_1^+$),($4_1^+ \rightarrow 2_1^+$),($4_2^+ \rightarrow 2_2^+$), ($4_3^+ \rightarrow 2_1^+$),and($6_1^+ \rightarrow 4_1^+$).

Figure (1) shows the relation between the electric transitions probability $B(E2)$ for the transitions ($2_1^+ \rightarrow 0_1^+$) , ($4_1^+ \rightarrow 2_1^+$),($6_1^+ \rightarrow 4_1^+$),($8_1^+ \rightarrow 6_1^+$) as a function of angular momentum $L+2 \rightarrow L$. It is noticed in this figure that the highest probability happened at transition ($6_1^+ \rightarrow 4_1^+$). This means that the strong $B(E2)$ happened at this transition ,also this figure shows very good agreement between present work and experimental data .

3-The electric quadrupole moments:

The electric quadrupole moments can be calculated from equation (8)by using the same parameters ($\delta 0$ and $\delta 1$)of $B(E2)$. The calculated values of (QL)show that these values are depending on $\delta 1$ – value more than($\delta 0$) and both of them depends on total number of bosons(N).

Table (5) shows the values of QL where $L=2$ to 6 , $i=1$ to 10 .

These values have been compared with experimental data and gives very perfect agreement of the first excited state

(2_1^+) and somehow small in second excited state (2_2^+).

Figure (2) explain the shape deformation of angular momentum $2_1^+ \rightarrow 2_{10}^+$ for nucleus understudy, which has a prolate type of deformation at state ($2_1^+, 2_3^+, 2_5^+, 2_7^+, 2_8^+$, and 2_9^+), This is agreeing with experimental shape and value in the state (2_1^+), while it has an oblate type at states ($2_2^+, 2_4^+, 2_6^+$, and 2_{10}^+).

Figure (3) same as in figure (2) but for $L=3_1^+ \rightarrow 3_{10}^+$. This figure shows the nucleus has an oblate type in ($3_1^+, 3_2^+, 3_3^+$) states, but the (3_4^+) state has prolate type, and has $QL=0$ in other

states. While in the figure (4) has prolate type in states ($4_1^+, 4_3^+, 4_6^+, 4_7^+, 4_8^+$, and 4_9^+) and an oblate type in another state.

Figure (5) shows that it has prolate type in states ($5_1^+, 5_4^+, 5_5^+$), while it has an oblate type in state ($5_2^+, 5_3^+$).

Figure (6) shows the nucleus has an oblate type in all states except has an oblate type in (6_3^+) state.

REFERENCES

- 1-Arima A. and Iachello F.; Phys .Lett. B, Vol. 53,p.309 (1974).
- 2-Walter P.;"An Introduction to the IBM of the atomic nucleus" part 1, Walter P.(4-8) (1998).
- 3-Casten R.F., and Warner D.D, "The interaction boson approximation" Rev modern.Phys.Vol.60,No.2,P.389 (1988).
- 4-Arima A. and Iachello F.," The interaction boson model ,"Ed. Iachello F., Pub. Cambridge university ,press Cambridge, England,P.(1-133) (1987).
- 5-Alenicheva T.V., Kabina P., Mitropolsky I.A., and Tyukavina T.M. ; IAEA Nuclear data section, Wagramer strasse5,A-1400 Viena , INDC (CCP) ,P.439 (2004).
- 6-Mariscotti M.A.J., Gertude Scharff-Gold Haber, and Brain Buck; phys. Rev.Vol.178,P.1864 (1969).
- 7-Krane K.S.," Introductory nuclear physics," Ed, Halliday,D. , Pub. John, Wiley, P.141-144 (1987).
- 8-Iman T.AL-Alawy:E0,M1,E2 Transitions of collective levels below 1.821Mev in Pt-196,:Al-Mustanisiriya J.Sci. Vol.11,No.1,P.146-160(2000).
- 9- Iman T.AL-Alawy,Khalid S.I.,and Firas A. A.,:The electric quadrupole moments,magnetic moments, g-factor and delta mixing ratios for deformed Yb(A=176) nucleus of dynamical symmetrySU(3)-SU(5).Accepted in Journal of AL-Mustansera University.2005.
- 10- Aobaid A.K.;Studying the effect of moment of inertia on the nuclear structure of some even-even nuclei,; (ph.D. thesis sub. to Al-Mustansiriya university(2006)
- 11-Scholten,O.,F.,Lachelo F,and Arima A. Phys. (N.Y) Vol.115, P.325 (1978).
- 12-Bhat M.R.,:Nuclear data sheets for A=70.:Vol.51 No.1 P.95(1987).
- 13-Sakai M.," Atomic data and nuclear data tables,"Vol.31, No.3, P.399-432 (1984).

Table(1):Selection rules and quadrupole moments in different dynamical symmetries[23]

Chain	operators	selection rule	Quadrupole moments
SU(5)	$[\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}]^{(2)}$ $[\hat{d}^\dagger \times \hat{d}]^{(2)}$	$\Delta n_d = \pm 1, \Delta v = \pm 1$ $\Delta n_d = 0, \Delta v = 0, \pm 2$	$Q_L = 0.676\delta_1 \sqrt{L/14}$
SU(3)	$[\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}]^{(2)}$ $[\hat{d}^\dagger \times \hat{d}]^{(2)}$	$\Delta \sigma = \pm 1, \Delta \tau = \pm 1$ $\Delta \sigma = 0, \Delta \tau = 0, \pm 2$	$Q_L = -1.121\delta_0 (L / (2L+3)(4N+3))$
O(6)	$[\hat{d}^\dagger \times \hat{s} + \hat{s}^\dagger \times \hat{d}]^{(2)}$ $[\hat{d}^\dagger \times \hat{d}]^{(2)}$	$\Delta \lambda = \Delta \mu = 0$ $\Delta \lambda = \Delta \mu = 0$ or $\Delta \lambda = \pm 4, \Delta \mu = \pm 4$	$Q_L = 0$

Table(2):Ideal energy ratios of three chains[3] compared with experimental[12,13] and theoretical values .

Valeus	$E(4_1^+)/E(2_1^+)$	$E(6_1^+)/E(2_1^+)$	$E(8_1^+)/E(2_1^+)$
SU(5)	2	3	4
SU(3)	3.33	7	12
O(6)	2.5	4.5	7
Exp.. [12,13]	2.0721	3.1735	4.0459
Present work(pw)	2.0072	3.0234	4.0501

Table (3): The parameters of Hamiltonian operators for $^{70}_{32}Ge_{38}$ nucleus.

The Parameters	N_π	N_ν	N	ϵ (MeV)	$\hat{P}^\dagger \cdot \hat{P}$ (MeV)	\hat{L}^2 (MeV)	\hat{Q}^2 (MeV)	\hat{T}_3^2 (MeV)	\hat{T}_4^2 (MeV)	χ (MeV)
Values	2	5	7	0.9740	0.0000	0.0090	0.0200	0.0500	-0.1000	0.8200

Table (4): Theoretical energy levels, transition energy, reduced matrix element $\langle L_f || \hat{T}^{(E2)} || L_i \rangle$, and probabilities of electric transitions B(E2) compared with available experimental data

L_i^+	Energy level E(L) (MeV)		Spin sequence $L_i^+ - L_f^+$	Transition energy E_γ (MeV)		$\langle L_f \hat{T}^{(E2)} L_i \rangle$ (eb)	B(E2) (eb) ²	
	Exp.[12]	IBM-1		Exp.[12]	IBM-1		Exp.[12]	IBM-1
0_1^+	0.00	0.00	-	-	-	-	-	-
2_1^+	1.0392	1.0536	$2_1^+ \rightarrow 0_1^+$	1.0392	1.0536	0.5130	0.0525	0.0526
0_2^+	1.2154	1,4608	$0_2^+ \rightarrow 2_1^+$	0.1762	0.4072	0.2825	0.1200	0.0798
			$0_2^+ \rightarrow 0_1^+$	1,2154	1.4608	0.0000	0.0000	0.0000
2_2^+	1.7079	1.9443	$2_2^+ \rightarrow 0_2^+$	0.4925	0.4835	-0.1470	0.0625	0.0043
			$2_2^+ \rightarrow 2_1^+$	0.6687	0.8907	0.4915	0.2775	0.0482
			$2_2^+ \rightarrow 0_1^+$	1.7079	1.9443	-0.0133	0.0025	0.0003
4_1^+	2.1534	2.1148	$4_1^+ \rightarrow 2_2^+$	0.4455	0.1705	-0.1279	-	0.0018
			$4_1^+ \rightarrow 2_1^+$	1.1142	1.0612	0.8512	0.0600	0.0665
2_3^+	2.1574	2.1949	$2_3^+ \rightarrow 2_2^+$	0.4495	0.2506	0.1974	-	0.0078
			$2_3^+ \rightarrow 0_2^+$	0.9470	0.7341	-0.2574	-	0.0132
			$2_3^+ \rightarrow 2_1^+$	1.1182	1.1413	-0.4306	-	0.0371
			$2_3^+ \rightarrow 0_1^+$	2.1574	2.1949	-0.0298	-	0.0002
0_3^+	2,3069	2.2099	$0_3^+ \rightarrow 2_2^+$	0.5990	0.2656	0.1268	0.1200	0.0161
			$0_3^+ \rightarrow 0_2^+$	1.0915	0.7491	0.0000	0.0000	0.0000
			$0_3^+ \rightarrow 2_1^+$	1.2677	1.1563	-0.0662	0.0350	0.0044
			$0_3^+ \rightarrow 0_1^+$	2.3063	2.2099	0.0000	-	0.0000
3_1^+	2.4515	2.8507	$3_1^+ \rightarrow 2_3^+$	0.2941	0.6558	-0.0551	-	0.0040
			$3_1^+ \rightarrow 4_1^+$	0.2981	0.7359	-0.3289	-	0.0154
			$3_1^+ \rightarrow 2_2^+$	0.7436	0.9064	0.5607	-	0.5449
			$3_1^+ \rightarrow 2_1^+$	1.4123	1.7971	-0.0006	-	0.5E-6
2_4^+	2.5356	2.4970	$2_4^+ \rightarrow 2_2^+$	0.8277	0.5527	0.1835	-	0.0067
			$2_4^+ \rightarrow 0_2^+$	1.3202	1.0362	0.3433	-	0.0236
			$2_4^+ \rightarrow 2_1^+$	1.4964	1.4434	0.0355	-	0.0002
4_2^+	2,8067	2.8099	$4_2^+ \rightarrow 4_1^+$	0.6533	0.6951	-0.2185	-	0.0053
			$4_2^+ \rightarrow 2_2^+$	1.0988	0.8656	-0.3693	0.0725	0.0152

Table(4):To be continued(2/3):

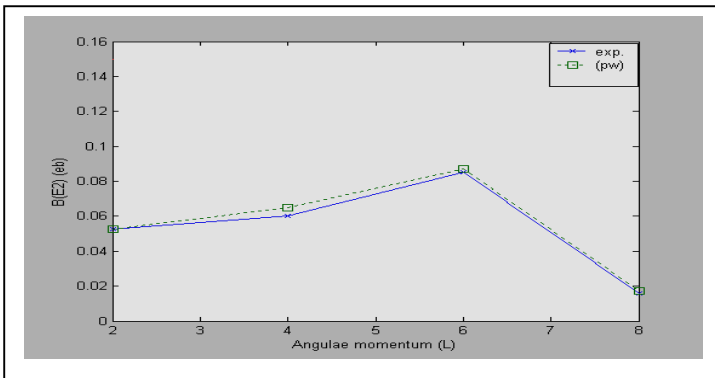
L_i^+	Energy level E(L) (MeV)		Spin sequence $L_i^+ - L_f^+$	Transition energy $E_\gamma(\text{MeV})$		$L_f \parallel \hat{T}^{(E2)} \parallel L_i \rangle$ (eb)	B(E2) (eb) ²	
	Exp.[12]	IBM-1		Exp.[12]	IBM-1		Exp.[12]	IBM-1
2_5^+	2.8877	2.8566	$2_5^+ \rightarrow 2_3^+$	0.7303	0.6617	0.0560	-	0.0006
2_6^+	2,9452	2.8734	$2_6^+ \rightarrow 2_2^+$	1.2373	0.9291	0.0999	-	0.0020
3_2^+	3.0468	3.2326	$3_2^+ \rightarrow 4_2^+$	0.2401	0.4227	-0.4120	-	0.0242
			$3_2^+ \rightarrow 3_1^+$	0.5953	0.3819	0.008E-6	-	0.7E-8
			$3_2^+ \rightarrow 2_3^+$	0.8894	1.0377	-0.4748	-	0.0322
			$3_2^+ \rightarrow 4_1^+$	0.8934	1.1178	-0.3028	-	0.0131
			$3_2^+ \rightarrow 2_2^+$	1.3389	1.2883	0.2839	-	0.0115
			$3_2^+ \rightarrow 2_1^+$	2.0076	2.1790	-0.0028	-	0.0E-4
4_3^+	3.0588	3.0133	$4_3^+ \rightarrow 4_2^+$	0.2521	0.2034	0.0306	-	0.0001
			$4_3^+ \rightarrow 2_3^+$	0.9014	0.8184	-0.6178	-	0.0024
			$4_3^+ \rightarrow 4_1^+$	0.9054	0.8985	0.4959	-	0.0273
			$4_3^+ \rightarrow 2_1^+$	2.0196	1.9527	0.0207	0.0050	0.0048
0_4^+	3.1070	2.6974	$0_4^+ \rightarrow 2_2^+$	1.3991	0.7531	0.0662	-	0.0043
			$0_4^+ \rightarrow 2_1^+$	2.0678	1.6438	-0.0259	-	0.0007
4_4^+	3.1942	3.2604	$4_4^+ \rightarrow 2_1^+$	2.1550	2.2068	-0.0815	-	0.0007
6_1^+	3.2979	3.1855	$6_1^+ \rightarrow 4_1^+$	1.1445	1.0707	0.7008	0.0850	0.0878
4_5^+	3,3730	3.3856	$4_5^+ \rightarrow 4_1^+$	1.2183	2.3320	0.2703	-	0.0081
			$4_5^+ \rightarrow 2_1^+$	2.3334	2.3320	-0.0081	-	0.07E-5
2_7^+	3.4230	3.4840	$2_7^+ \rightarrow 2_1^+$	2.3838	2.4304	0.0289	-	0.0002
5_1^+	3.4560	3.7978	$5_1^+ \rightarrow 4_1^+$	1.3026	1,6830	-0.0551	-	0.0003
3_3^+	3.4824	3.7152	$3_3^+ \rightarrow 2_4^+$	0.9538	1.2182	0.0280	-	0.0001
			$3_3^+ \rightarrow 2_3^+$	1.3320	1.5203	0.0800	-	0.0009
			$3_3^+ \rightarrow 4_1^+$	1.3360	1.6004	0.0690	-	0.0007
			$3_3^+ \rightarrow 2_2^+$	1.7815	1.7709	-0.0676	-	0.0006
			$3_3^+ \rightarrow 2_1^+$	2.4502	2.6616	0.0027	-	0.01E-4
6_2^+	3.6670	3.5401	$6_2^+ \rightarrow 4_1^+$	1.5136	1.4253	0.7662	-	0.0451

Table(4):To be continued(3/3):

L_i^+	Energy level E(L) (MeV)		Spin sequence $L_i^+ - L_f^+$	Transition energy $E_\gamma(\text{MeV})$		$\langle L_f \parallel \hat{T}^{(E2)} \parallel L_i \rangle$ (eb)	B(E2) (eb) ²	
	Exp.[12]	IBM-1		Exp.[12]	IBM-1		Exp.[12]	IBM-1
4_6^+	3.6775	3.7196	$4_6^+ \rightarrow 4_1^+$	1.5241	1.6048	0.0845	-	0.0008
			$4_6^+ \rightarrow 2_1^+$	2.6383	2.6660	0.0122	-	0.16E-4
6_3^+	3.7534	3.8467	$6_3^+ \rightarrow 4_2^+$	0.9467	1.0368	-0.3460	0.0675	0.0092
4_7^+	3.9280	3.9266	$4_7^+ \rightarrow 2_1^+$	2.8888	2.8730	-0.0152	-	0.25E-4
8_1^+	4.2045	4.2672	$8_1^+ \rightarrow 6_1^+$	0.9066	1.0817	0.5417	0.0162	0.0173
7_1^+	4.2991	4.6746	$7_1^+ \rightarrow 6_1^+$	1.0012	1,4891	0.3881	0.0002	0.0100
8_2^+	4.4316	4.6186	$8_2^+ \rightarrow 6_1^+$	1.1337	1.4331	0.1939	0.1075	0.0022
8_3^+	4.8521	4.9204	$8_3^+ \rightarrow 8_1^+$	0.6476	0.6532	-0.3870	-	0.0088
8_4^+	5.2994	5.3211	$8_4^+ \rightarrow 8_2^+$	0.8678	0.7025	-0.7157	-	0.0301
10_1^+	5.5399	5.3281	$10_1^+ \rightarrow 8_2^+$	0.1083	0.7095	0.1386	-	0.0009

Table (5):The calculated and experimental values of electric quadrupole moments.

Q_L	Value(eb)	Q_L	value(eb)	Q_L	value(eb)	Q_L	value(eb)	Q_L	value(eb)
Q_{2_1}	0.0373 +0.03 ^[11]	Q_{3_1}	-0,18x10 ⁻⁸	Q_{4_1}	0.1336	Q_{5_1}	0.1023	Q_{6_1}	0.7407
Q_{2_2}	-0.0472	Q_{3_2}	-0.07x10 ⁻⁸	Q_{4_2}	-0.0927	Q_{5_2}	-0.0351	Q_{6_2}	0.1485
Q_{2_3}	0.3996	Q_{3_3}	0.10x10 ⁻⁷	Q_{4_3}	0.3032	Q_{5_3}	-0.1754	Q_{6_3}	-0.4613
Q_{2_4}	-0.1975	Q_{3_4}	0.26x10 ⁻⁸	Q_{4_4}	-0.0953	Q_{5_4}	0.2764	Q_{6_4}	0.3578
Q_{2_5}	0.4186	Q_{3_5}	Q_{4_5}	.0.1555	Q_{5_5}	0.2165	Q_{6_5}	0.5516
Q_{2_6}	-0.6701	Q_{3_6}	Q_{4_6}	0.2102	Q_{5_6}	Q_{6_6}	0.1100
Q_{2_7}	0.4438	Q_{3_7}	Q_{4_7}	0.0226	Q_{5_7}	Q_{6_7}	0.6991
Q_{2_8}	0.3640	Q_{3_8}	Q_{4_8}	0.3106	Q_{5_8}	Q_{6_8}	0.1271
Q_{2_9}	0.0157	Q_{3_9}	Q_{4_9}	0.9742	Q_{5_9}	Q_{6_9}	0.4360
$Q_{2_{10}}$	-0.1385	$Q_{3_{10}}$	$Q_{4_{10}}$	-0.0282	$Q_{5_{10}}$	$Q_{6_{10}}$	0.5491



Figure(1):Electric transition probability B(E2) with angular momentum

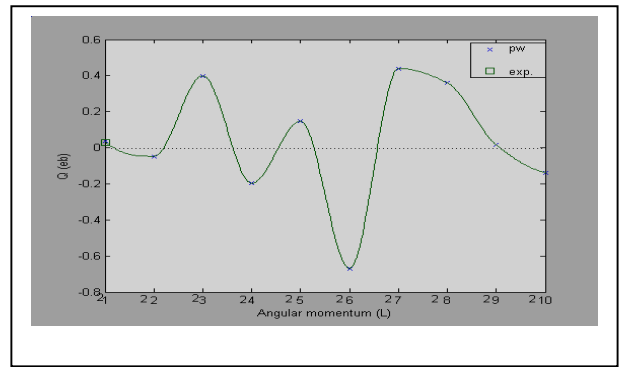


Figure (2): The electric quadrupole moment as a function of angular momentum L=2₁ to 2₁₀.

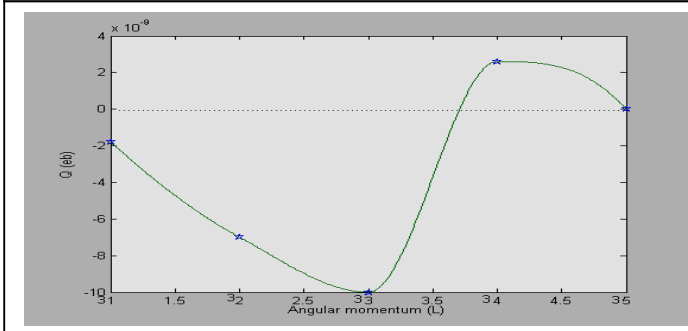
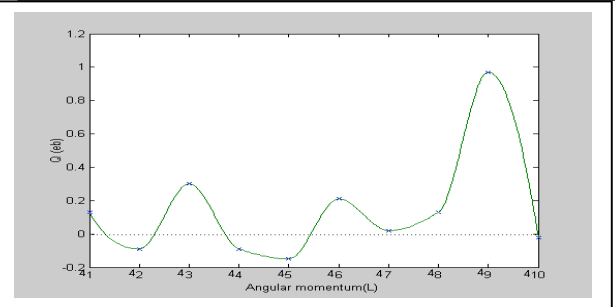
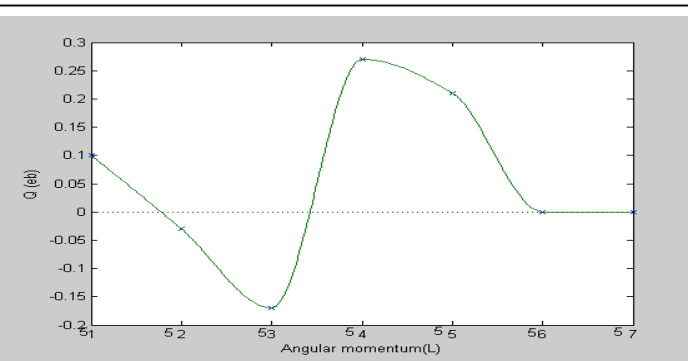


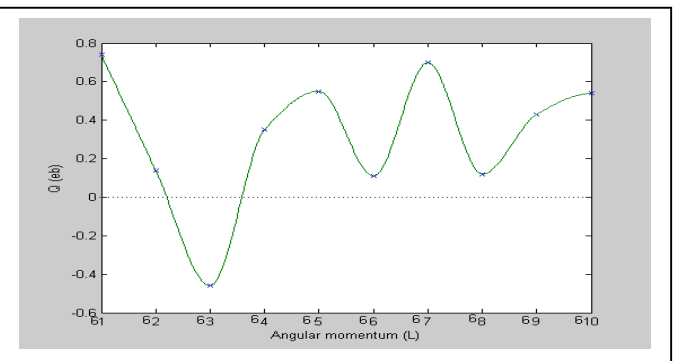
Figure (3): Same as in fig. (2) but for L=3₁ to 3₅.



Figure(4):The electric quadrupole moment as a function of angular momentum L=4₁ to 4₁₀



Figure(5):The electric quadrupole moment as a function of angular momentum L=5₁ to 5₇



Figure(6):The electric quadrupole moment as a function of angular momentum L=6₁ to 6₁₀



E.mail: scicoll@yahoo.com

(IBM-1)

SU(5)-SU(3)